



University of Science and Technology

Faculty of Engineering

first Year - Semester (1)

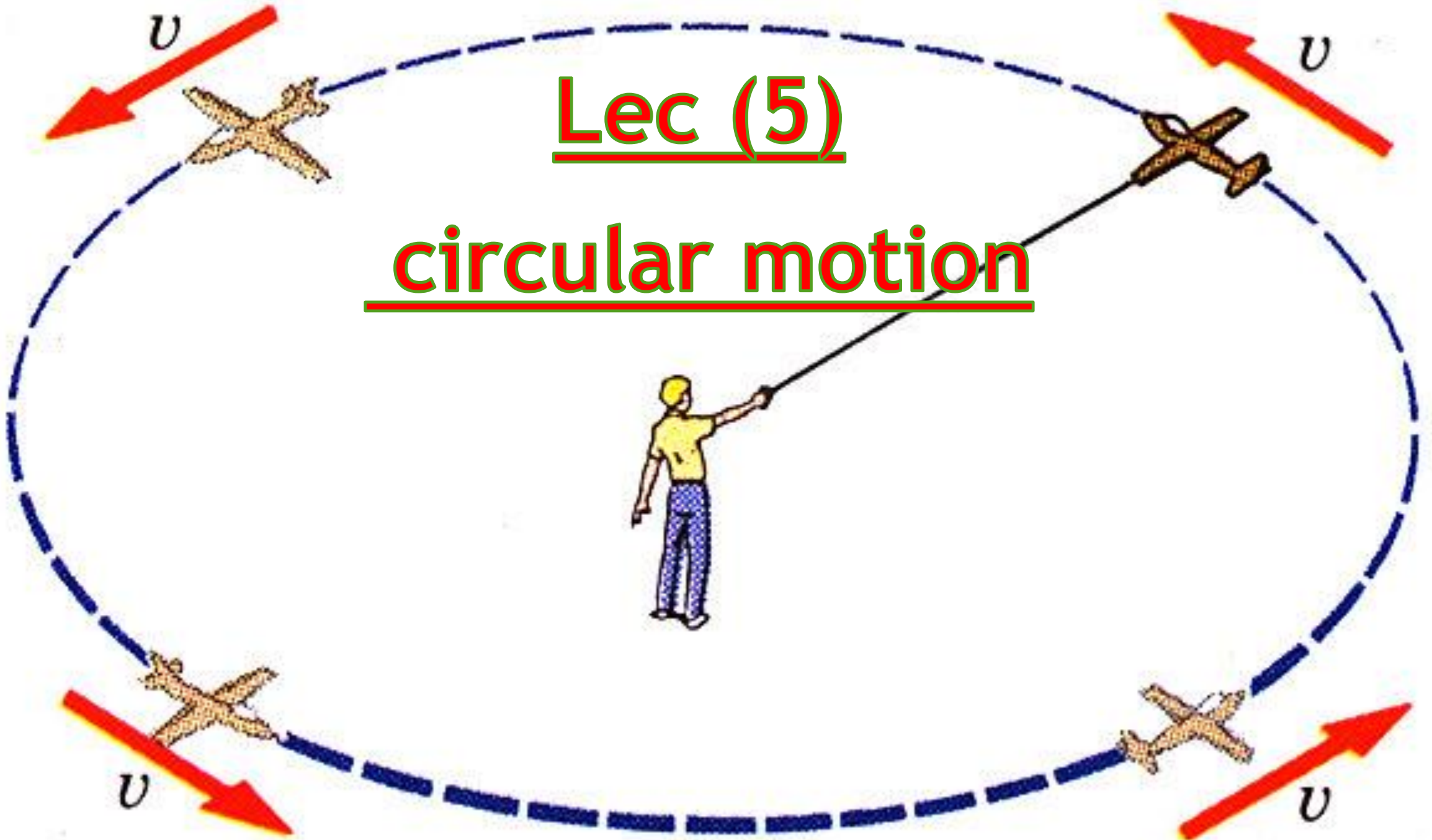
physics (1)

Dr.Moawia Ibrahim hamedelnil



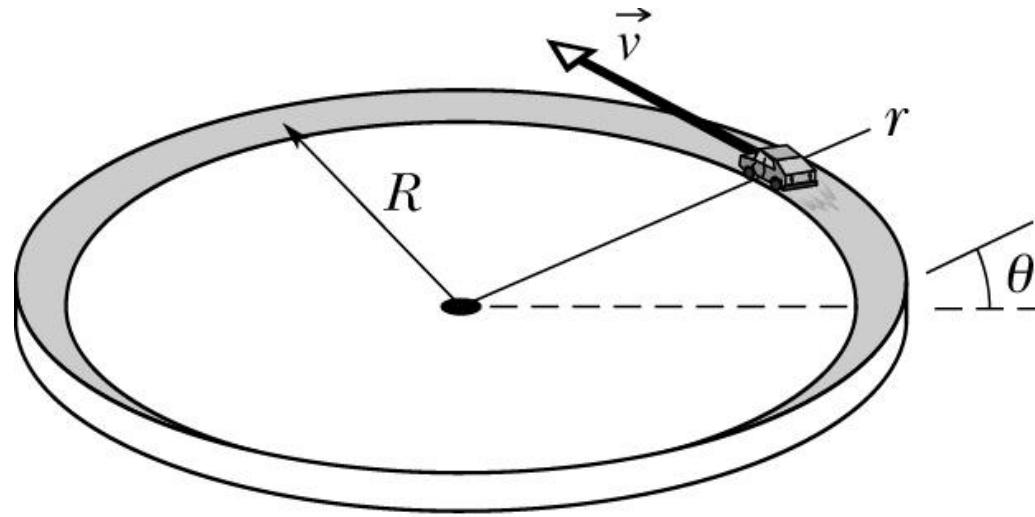
Lec (5)

circular motion



circular motion

- In uniform Circular motion a body travels at a constant speed on a circular path.



arc length = radius x Angle in radians

$$s = r \theta$$

$$1 \text{ rev} = 360^\circ = 2\pi \text{ rad}$$

*** Angular velocity = angular displacement / time**

$$\omega = \theta / t$$

*** Linear velocity = (angular velocity)(radius of circle)**

$$V = \omega r$$

*** The period (T) of revolution is the time an object takes to complete one revolution**

$$T = 2\pi / \omega$$

$$V = 2\pi r / T$$

* Centripetal acceleration (a)

$$a_c = v^2 / r$$

* Centripetal Force (F)

$$F_c = mv^2 / r$$

* angular acceleration(α)

Angular acceleration = angular velocity change / time

$$\alpha = \omega_f - \omega_0 / t$$

* angular displacement

$$\theta = \omega_0 t + 1/2 \alpha t^2$$

$$\omega_f^2 = \omega_0^2 + 2\alpha\theta$$

Linear Motion with a Constant
(Variables: x and v)

$$v = v_i + at$$

$$\Delta x = v_i t + \frac{1}{2} at^2$$

$$v^2 = v_i^2 + 2a\Delta x$$

Rotational Motion about a Fixed Axis with α Constant (Variables: θ and ω)

$$\omega = \omega_i + \alpha t \quad [7.7]$$

$$\Delta \theta = \omega_i t + \frac{1}{2} \alpha t^2 \quad [7.8]$$

$$\omega^2 = \omega_i^2 + 2\alpha \Delta \theta \quad [7.9]$$

$$a = \frac{v^2}{r} = \frac{(r\omega)^2}{r} = \frac{r^2\omega^2}{r} = r\omega^2$$

$$F = ma = mr\omega^2$$

Linear

Angular

Quantity	unit	Quantity	unit
Displacement (x)	m	Angular displacement (Θ)	Rad
Velocity (v)	m/s	Angular velocity (ω)	Rad/sec
Acceleration (a)	m/sec ²	Angular acceleration (α)	Rad/sec ²
Mass (m)	Kg	Moment of inertia (I)	Kg * m ²
Force (F)	Kg * m/s or N	Torque (t)	N*m

Law of gravitation

$$F_g = G \frac{m_1 m_2}{r^2}$$

G = universal gravitational constant

$$= 6.67 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$$

m_1 and m_2 = masses of interacting bodies

r = distance between their centres

SOLVED PROBLEM (1) :

(a) Express 6 rev in radians.

(b) How many revolutions are equivalent to 10 rad?

$$(a) \quad \theta = (8^\circ) \left(\frac{2\pi \text{ rad}}{360^\circ} \right) = 0.14 \text{ rad}$$

$$(b) \quad \theta = (2.5 \text{ rad}) \left(\frac{360^\circ}{2\pi \text{ rad}} \right) = 143 \text{ rad}$$

SOLVED PROBLEM (2) :

A 1000-kg car rounds a turn of radius 30 m at a velocity of 9 m/s. (a) How much centripetal force is required?

$$F_c = \frac{mv^2}{r} = \frac{(1000 \text{ kg})(9 \text{ m/s})^2}{30 \text{ m}} = 2700 \text{ N}$$

SOLVED PROBLEM (3) :

An engine requires 5 s to go from its idling speed of 600 rev/min to 1200 rev/min. (a) What is its angular acceleration? (b) How many revolutions does it make in this period?

(a) The initial and final angular velocities of the engine are, respectively,

$$\omega_0 = (600 \text{ rev/min}) \left(\frac{2\pi \text{ rad/rev}}{60 \text{ s/min}} \right) = 63 \text{ rad/s}$$

$$\omega_f = (1200 \text{ rev/min}) \left(\frac{2\pi \text{ rad/rev}}{60 \text{ s/min}} \right) = 126 \text{ rad/s}$$

and so its angular acceleration is

$$\alpha = \frac{\omega_f - \omega_0}{t} = \frac{126 \text{ rad/s} - 63 \text{ rad/s}}{5 \text{ s}} = 12.6 \text{ rad/s}^2$$

(b) The angle through which the engine turns is

$$\begin{aligned} \theta &= \omega_0 t + \frac{1}{2} \alpha t^2 = (63 \text{ rad/s})(5 \text{ s}) + \left(\frac{1}{2}\right)(12.6 \text{ rad/s}^2)(5 \text{ s})^2 \\ &= 472.5 \text{ rad} \end{aligned}$$

Since there are 2π rad in 1 rev,

$$\theta = \frac{472.5 \text{ rad}}{2\pi \text{ rad/rev}} = 75.2 \text{ rev}$$

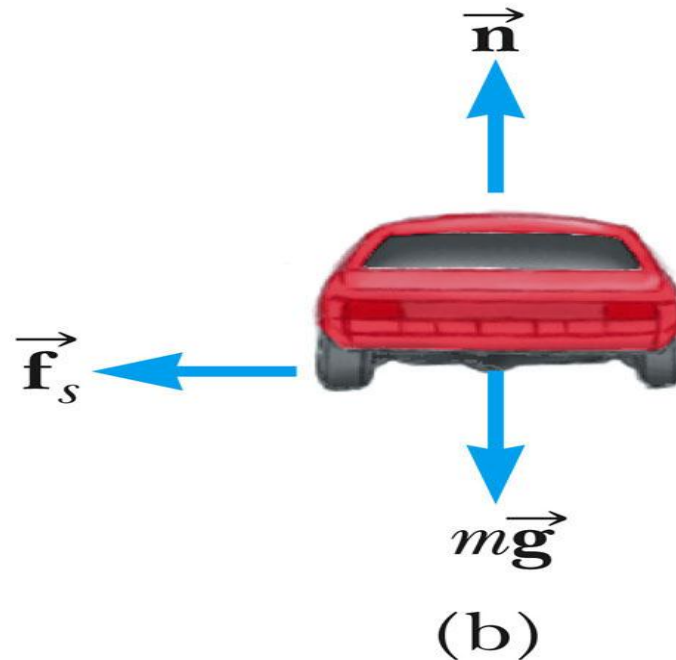
Centripetal Acceleration

$$a_c = \frac{v^2}{r} \quad (\textbf{centripetal acceleration})$$

$$v = \frac{2\pi r}{T} \quad (\textbf{tangential velocity})$$

Level Curves

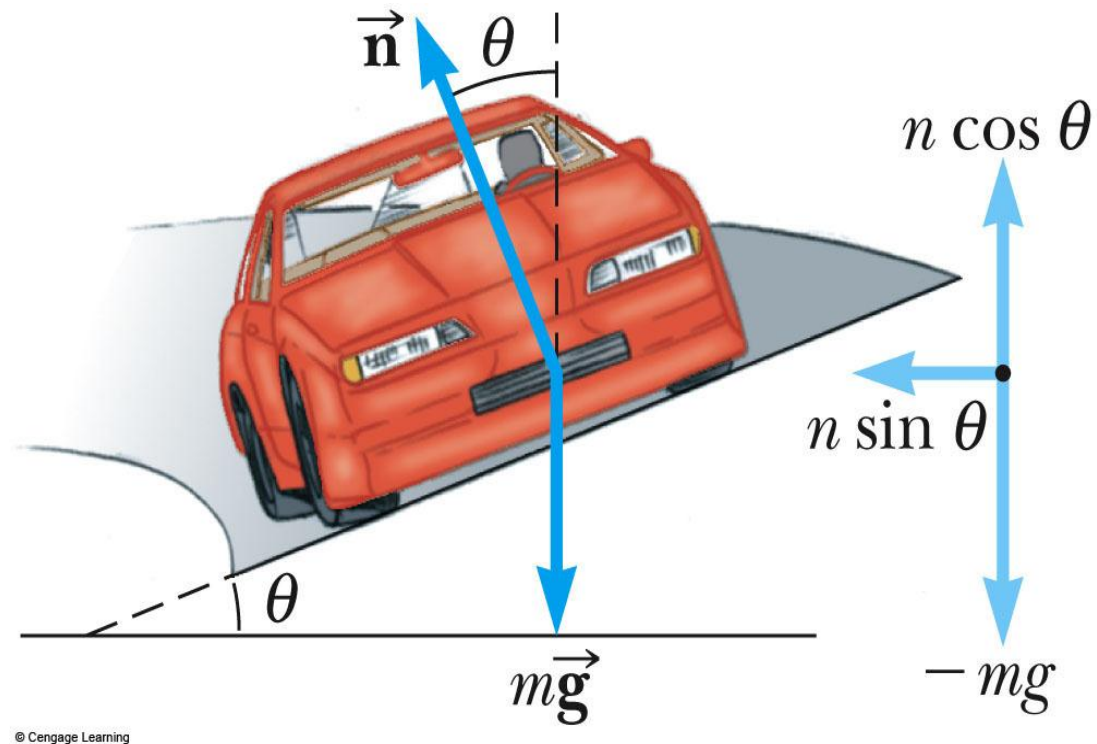
- Friction is the force that produces the centripetal acceleration
- Can find the frictional force, μ , or v



$$v = \sqrt{\mu rg}$$

Banked Curves

- A component of the normal force adds to the frictional force to allow higher speeds



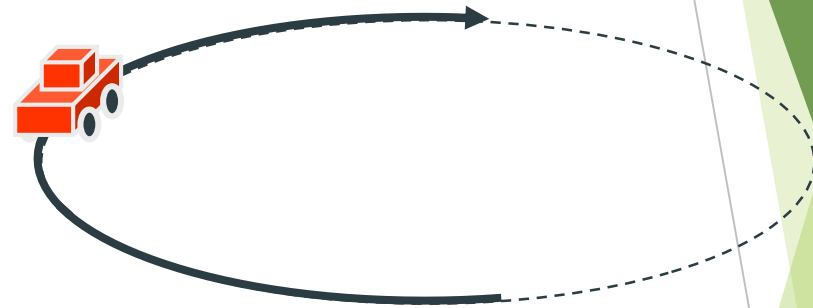
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$$\tan \theta = \frac{v^2}{rg}$$

$$\text{or } a_c = g \tan \theta$$

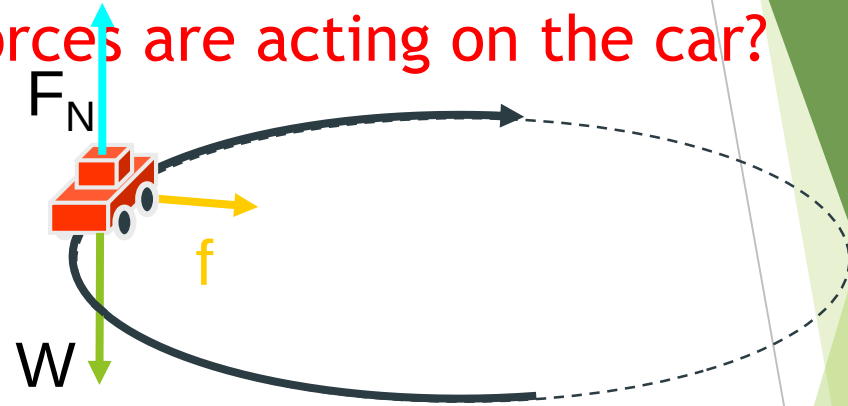
Consider the following situation: You are driving a car with constant speed around a horizontal circular track. On a piece of paper, draw a Free Body Diagram (FBD) for the car. **How many forces are acting on the car?**

- A) 1
- B) 2
- C) 3
- D) 4



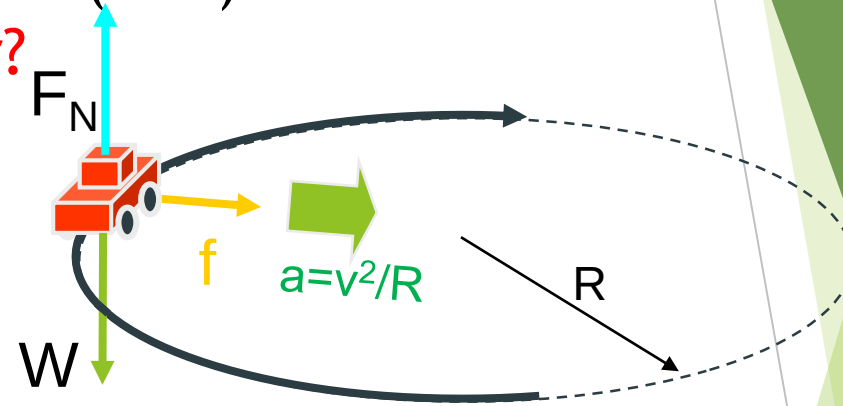
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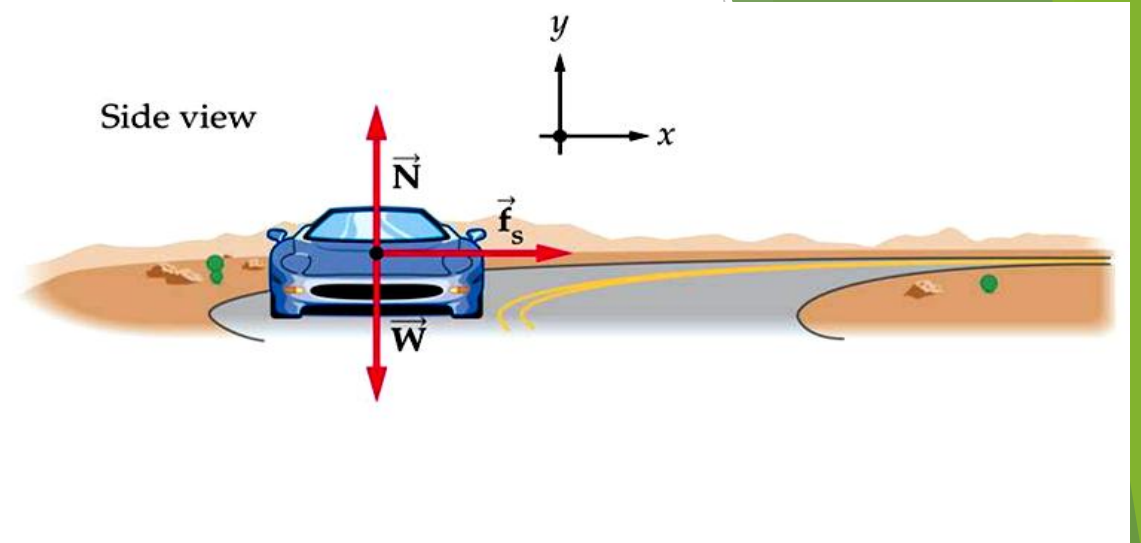
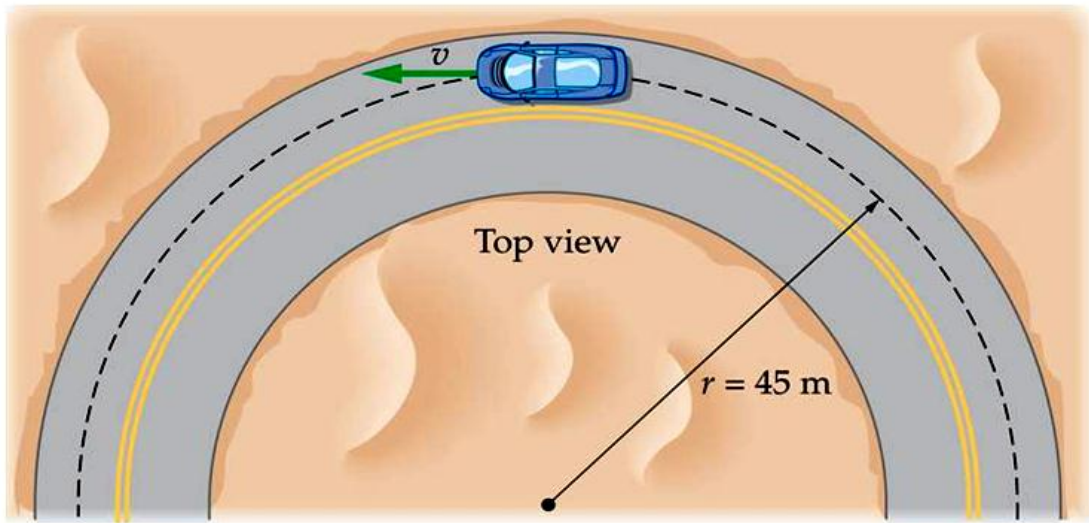
Consider the following situation: You are driving a car with constant speed around a horizontal circular track. On a piece of paper, draw a Free Body Diagram (FBD) for the car. **How many forces are acting on the car?**

- A) 1 0%
- B) 2 28%
- C) 3 44% ← correct
- D) 4 28%



$$\Sigma \mathbf{F} = m\mathbf{a} = mv^2/R$$

“Gravity, Normal Force, Friction”
“ F_n = Normal Force, W = Weight,
the force of gravity, f = centripetal force.”



A 1,200 kg car rounds a corner of radius $r = 45.0$ m. If the coefficient of friction between the tires and the road is $\mu_s = 0.82$, **what is the maximum speed the car can have on the curve without skidding?**

$$\sum F_x = f_s$$

$$F_{netx} = \mu_s N$$

$$\therefore \mu_s \cancel{mg} = \cancel{m} \frac{v^2}{r}$$

$$F_{net} = \mu_s mg$$

$$F_{net} = m \frac{v^2}{r}$$

$$\sum \vec{F}_y = 0$$

$$N = w$$

$$N = mg$$

$$v = \sqrt{\mu_s r g} = \sqrt{(0.82)(45.0 \text{ m})(9.81 \text{ m/s}^2)} = 19.0 \text{ m/s}$$

Question: How does this result depend on the mass of the car?